

StatisticalHelp Al

Helping health experts know enough statistical methodology to safely analyse their data with <u>www.statsdirect.com</u> since 1987. Next Conversational Data Analytics with generative Als...



www.liverpool.ac.uk/statisticalhelp



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What you will learn from this session

- Public health and healthcare needs to mobilise data into action
- The importance of fusing health (or other domain context) and statistical methodology knowledge when analysing data
- Learning from <u>www.statsdirect.com</u> software development journey since 1987 of how to **trap** common statistical misconceptions and help the user make a reliable inference
- Liverpool's Civic Health Innovation Labs' commitment to research and apply Conversational Data Analytics Al
- Building a global reference site of 'statistical conversations' to test and harness generative Als data analytic utility



The need

The following slides show examples of turning data into action in response to the COVID-19 pandemic and how healthcare AI can learn from data in joined-up ways with continuous learning loops linked across personal health, care provider and population health management...



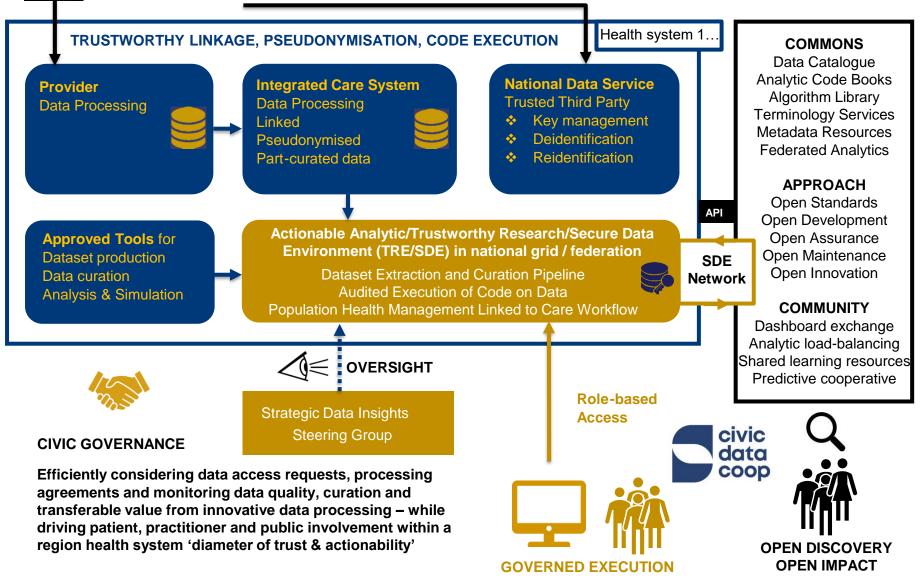








CIVIC DATA COOPERATIVE



- Ainsworth J, Buchan I. Combining Health Data Uses to Ignite Health System Learning. Methods Inf Med. 2015;54(6):479-87
- Buchan I, National Grid of Civic Data Cooperatives for Health in The Health of the Nation February 2020 www.liverpool.ac.uk/coronavirus/research-and-analysis/covid-smart-pilot/

Mobilising data into action...

Spring 2019 **Public Support for Data Uses** CivicDataCooperative.com

Summer 2020

Covid-19 intelligence system in 90 days for 2.7m population

CIPHA.nhs.uk

Autumn 2020 World-first voluntary mass testing Covid-SMART

Spring 2021 First reopening of mass events First Dance

> Winter 2022 **Mental Health Mission** M-RIC

Winter 2023 / Spring 2024 Research Centre, Birth Cohort, **NHS Data-into-Action**

Covid-19 Wakeup Call for Action Ready Data

Tests & Cases

All Cheshire & Merseyside (C&M) residents tested at any Pillar 2 test site and non-C&M residents tested at a C&M test site

Note: this report does not include Pillar 1 data.

Note: positivity rate calculations do not follow PHE

18,274,586 Tests Completed (LFT+PCR)

2,439,026 Individuals Tested

(LFT+PCR)

Show Filters

803.196 Individuals Tested

Positive (LFT+PCR)

3.22% LFT Case Positivity Rate (Asymptomatic)

Clear Filters

PCR Case Positivity Rate (Symptomatic)

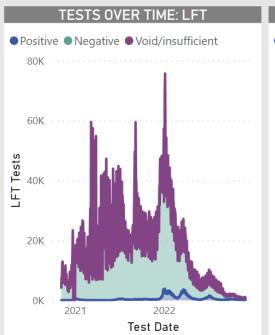
15.04%

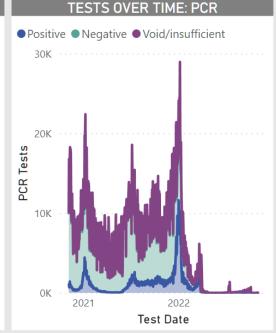
Filters Applied

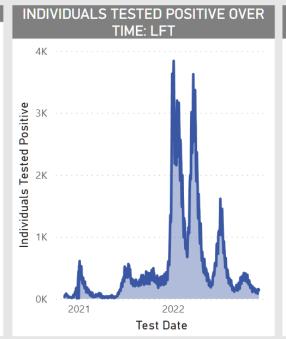
methodo	logy	•	
		TEST	COL
Test Kit	Tests Completed	Positive Tests	NI

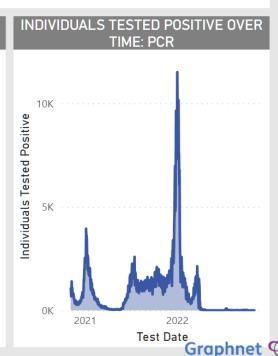
TEST COUNTS				
Test Kit	Tests Completed	Positive Tests	Negative Tests	Void / Insufficient Tests
	406,360	21,834	369,056	15,470
LFT	13,394,612	430,575	12,948,537	15,500
PCR	4,473,614	659,790	3,726,918	86,906
Total	18,274,586	1,112,199	17,044,511	117,876

INDIVIDUALS TESTED POSITIVE				
Test Kit	Individuals Tested	Individuals Tested Positive	Case Positivity Rate (Individuals)	
	115,833	21,137	5.59%	
LFT	1,666,102	315,295	3.22%	
PCR	1,585,738	610,445	15.04%	
Total	2,439,026	803,196	6.13%	









Near real-time covid testing data for 2.7m people of Cheshire & Merseyside

Linked to GP and partial hospital and social care records

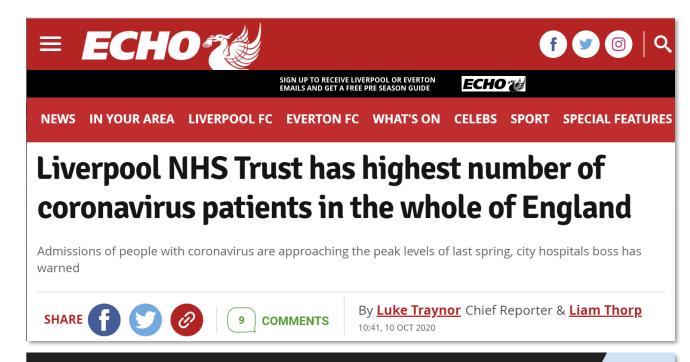
Dashboards for care, planning and research



Data available up to: 25/1/2029 10:40. Run by: buchan@liverpool.ac.uk on 8/12/2022 08:11; V1.9.0

Liverpool October 2020: Lives & Livelihoods

- COVID-19 deaths surge
- One of most deprived parts of UK Third of children born in poverty
- Job-losses surge from COVID-19 restrictions
- Visitors, hospitality and events form half of Liverpool's economy
- Lockdowns a public health hazard as well as SARS-CoV-2





Liverpool November 2020: Mass Testing Pilot

- World's first city-wide pilot of testing for people without COVID symptoms to save lives and livelihoods
- Quarter of population volunteered in a month despite external media negativity
- Case detection increased by a fifth
- Known case rate fell by a fifth
- Hospitalisation fell by a quarter



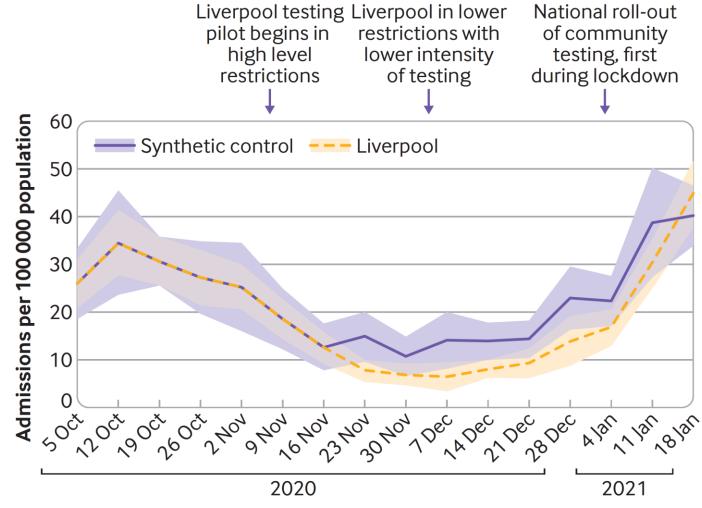


www.bmj.com/content/379/bmj-2022-071374

www.liverpool.ac.uk/coronavirus/research-and-analysis/covid-smart-pilot/

Impact of Mass Testing on Covid-19 Hospitalisations

- Synthetic control analysis making neighbourhoods similar in terms of background risks, epidemic and control measures
- Initial mass testing with military:
 43% (29% to 57%) reduction in COVID-19 hospital admissions
- Overall community testing pilot with handover to local services
 25% (11% to 35%) reduction



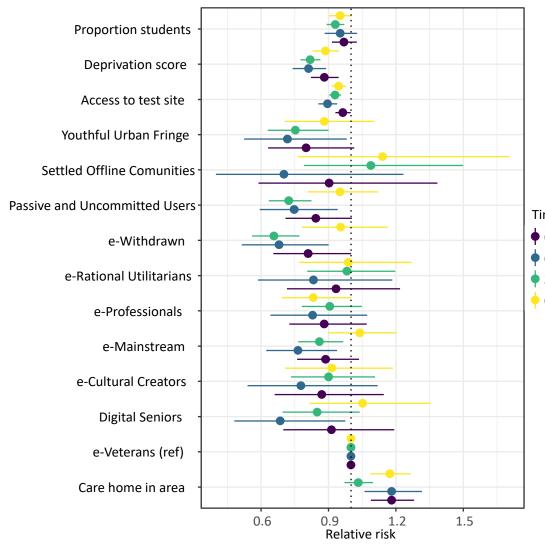
Results: https://www.bmj.com/content/379/bmj-2022-071374

Methodology: https://www.bmj.com/content/379/bmj.o2712

Policy impacts: www.liverpool.ac.uk/coronavirus/research-and-analysis/covid-smart-pilot/

Week start date

Digital Poverty -> Low Test Uptake: Need Universal Access



 Liverpool pilot demonstrated lower uptake of testing and higher infection rates among the most deprived and the digitally excluded (Internet User Classification of neighbourhoods)

Time period

- 6th Nov 26th Apr (total study period)
- 6th Nov 2nd Dec (#Let's all get tested)
- ◆ 3rd Dec 5th Jan (#Test before you go)
- 6th Jan 26th Apr (#Testing our front line)
 - Community testing roll-out advised to focus more on interactions of biology, behaviour and environment (end-to-end testing)
 - Need to reduce digital complexity
 - Isolation payments needed for those who can't afford to isolate

Digital Twin from Records or Self-experiment Avatar?









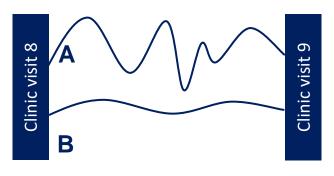






Sparse NHS records of clinical 'pit-stops'
Digital by-products of health, habits and self-care experiments
Rhythms of life to tap for discovery, engagement and intervention

Apps → **Avatar Skills and Measurement Based Care**

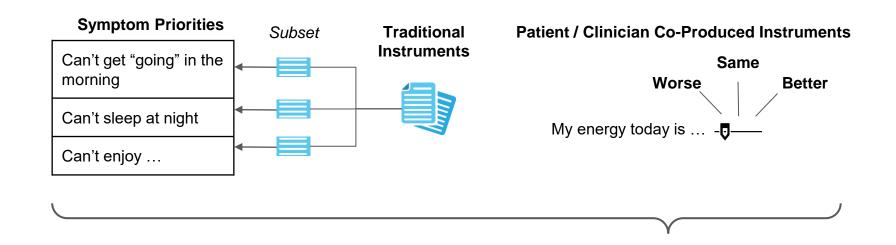


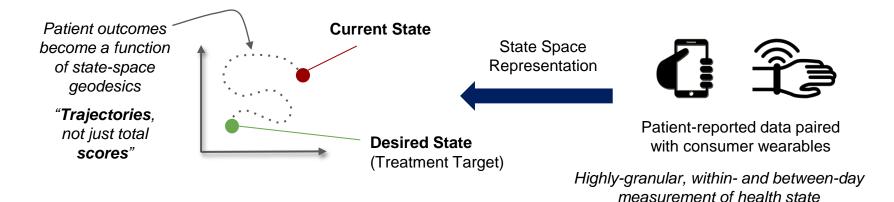
Two patients:

- Same diagnosis / treatment
- Different conditions / needs
- Key rhythms invisible to clinic

App market failure:

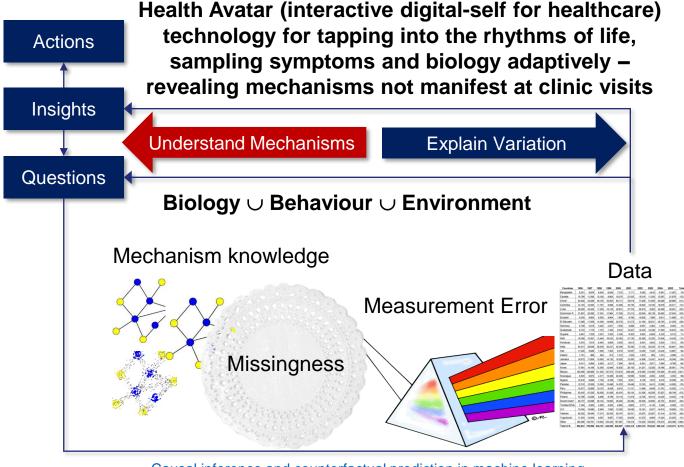
- Blizzard of apps for drugs, devices, clinics etc.
- Patient burden too high
- More people living longer with more than one condition
- Combinatorial explosion of complexity and confusion
- Lack of transparency & trust





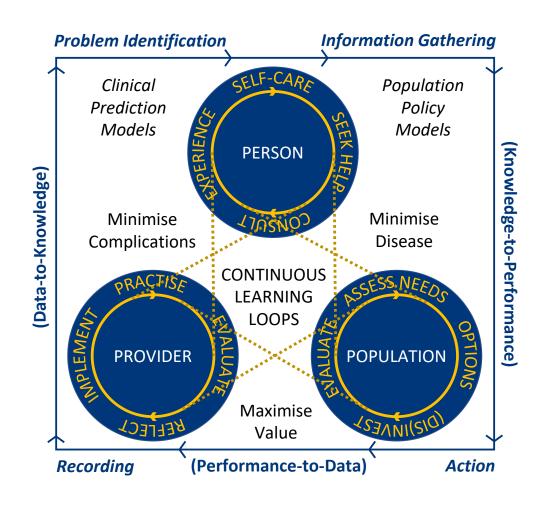
TREAT THE PATIENT NOT THE DIAGNOSIS
AND MANAGE THE JOURNEY NOT THE VISIT

Linked Digital Twins: Health Avatar & Learning Health System



Causal inference and counterfactual prediction in machine learning for actionable healthcare | Nature Machine Intelligence

Millions of health avatars training and testing Als in better care would reveal temporal (transdiagnostic) patterns and enable adaptive observation and serial experimentation for new discovery



The promise of 'learning health systems' will not be realised without 'discovery grade' data, causal inference and experiments

Optimising Healthcare Components vs Systems

Clinical Audit \rightarrow Governance (UK in 1980s/90s \rightarrow 00s)

Learning Health Systems (US rebranding in 2010s)

- More people living longer with multiple long-term conditions
- Due to affect 68% of >65-year-olds in UK by 2035 *
- Multi-condition pressures arise at younger ages in deprived areas
- Combined mental-physical problems more in young and deprived
- Existing system pressures higher in deprived areas
- Health and social care interdependency more in deprived areas
- Fewer resources for prevention accelerates compound pressures
- Climate/conflict/other world pressures denude available funds
- Population health management Als trained/tested in affluent areas

Specialist registries/databases

Crude predictive models (baseline risk factor loaded)

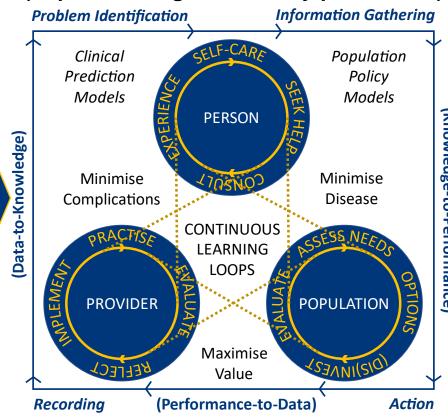
1-way translation (trials evidence into practice)

Integrated clinical records

Fuller longitudinal prediction (difficulty learning models from data)

2-way translation aim (+ practice-based evidence)

Health Systems (Pop. Health Mgt. Al industry push 2020s)



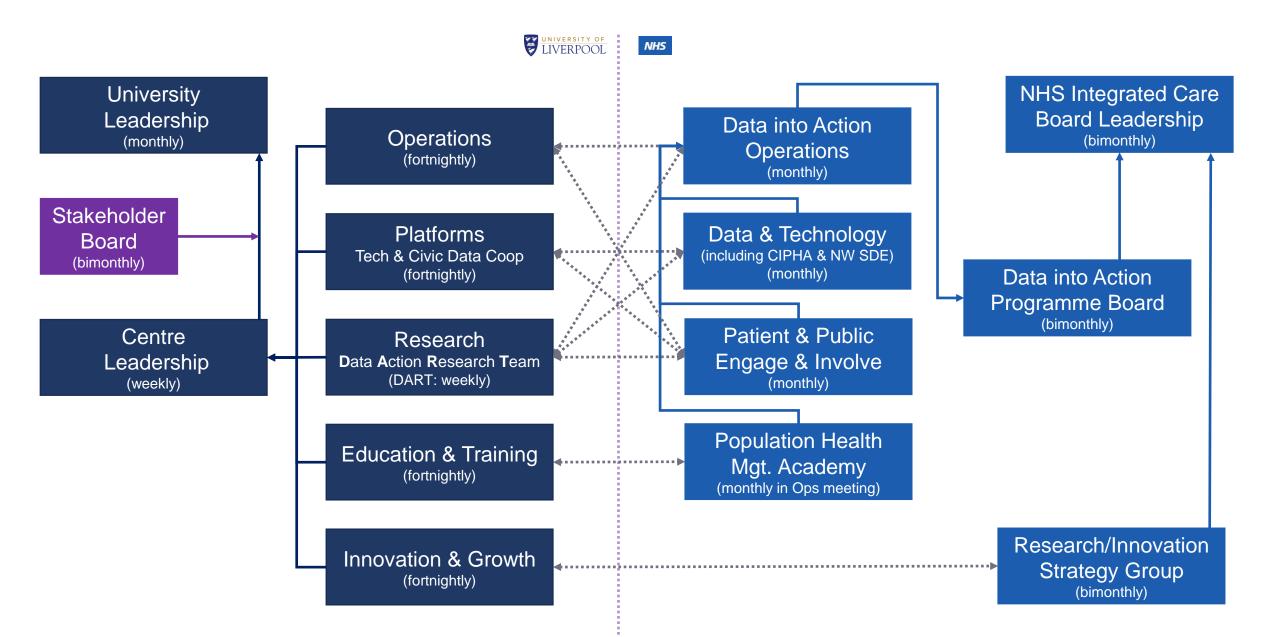
Wider civic (e.g. social care) data linkage

Multi-outcome prediction; complex interventions (system dynamics; causal machine learning)

Reverse-engineering actions to tackle escalating/compound pressures



CHIL Governance with NHS



Citizens Advice on Prescription Does it improve mental health?



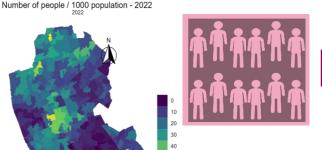






Large number of high need patients seen

- 65,000 people between 2018 and 2022
- 70% living in poverty
- 40% with at least 1 mental health problem
- 60% with multimorbidity
- Average 30 GP consultations per 100 clients in the 3 months before intervention



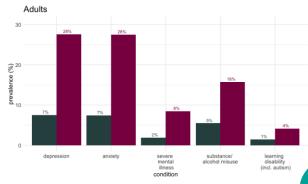
Routine linked-data cohort



Referral to
Citizens Advice
on Prescription



- Mental health care utilization:
- Antidepressant prescribing
- A&E attendances
- GP consultations
- Admissions



Cost per client was £141

Patient reported outcomes: EQ-5D, SWEMWBS



- Reduced anxiety and depression
- Improved wellbeing

Impacts

- Reduction in Antidepressant prescribing by 73 ADQs per person per quarter (95% CI 25-121)
- 7 fewer A&E attendances per 100 clients per quarter (2-11)





Innovation Labs

Return on investment: For every £1 invested in the CAP service, £6.50 of value was generated



Themes: global challenges; system data-action hungry

HEALTH & CARE SYSTEMS (pressure-resilience, equity, life-course, population health...)

C-GULL, PHIRST LiLaC, Data into Action, Round E're, SysteMatic, M-RIC, HDRC, GroundsWell, ARC NW Coast

MENTAL HEALTH (connected: digital, comorbidities, community/systems...)

M-RIC, Data Action Accelerator, CHI-Zone, 4M

INFECTION RESILIENCE (antimicrobial resistance, pandemic preparedness...)
AMR-X, Data Action Accelerator, CAMO-Net, FluVue, Pandemic Institute, BRIT, CHI-Zone, HPRU GI

MEDICINES OPTIMISATION (safety, genomics, companion-AI, polypharmacy, multimorbidity...)

<u>DynAlRx</u>, OLS Data Action Accelerator, CHI-Zone, <u>M-RIC</u>, <u>SysteMatic</u>

METHODS & INFRASTRUCTURE (training, methodology, digital infrastructure...)

CDC, M-RIC, HOD2, ARISTOTELES, CIPHA/SDE, Data Action Accelerator



CHIL Civic Health Innovation Labs

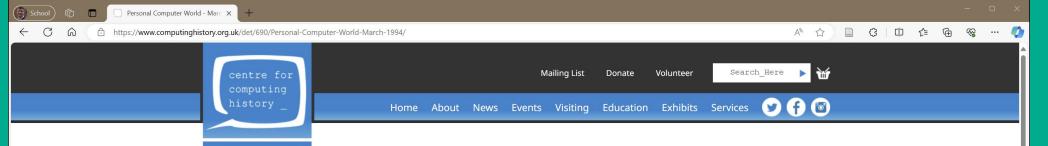
On opening in December 2023:

"Collaboration within the research sector is essential if we want to tackle some of the largest health and care problems facing the world today, and centres like this make that a reality."

Professor Lucy Chappell
Chief Scientific Adviser DHSC
and CEO of NIHR

'Safe Statistics' - wakeup call in late 1980s

- PC revolution: more health researchers and professionals could analyse their own data
- Statistical software was written for statisticians not application domain experts and could easily be misused
- Knowledge about mechanisms needed to set up the best analysis was in the brain of the domain expert
- Knowledge about statistical methods to use and how to interpret the results was in the brain of the statistician
- "Arcus ProStat" shareware (for MS DOS in BASIC 7.1, FORTRAN, assembler; no external) written as statistical knowledge support and data analytic tool for common/simple methods



Personal Computer World - March 1994

Home > Browse Our Collection > Magazines > Personal Computer World - 1994 > Personal Computer World

Apple PowerBook Duo 270c Caere OmniScan Windows

Virgin E DX2/66

Tracker for Windows

Trend Monitor e-Book

Ezio FlexScan F780i

OmniVerse 60

Texas TravelMate 4000E Win486DX2/50

Synergizer

Trust FC2614 Colour Scanner

Lexmark IJ4076 and LP4037 5E

Digital Soup

Q/Media for Windows

InfoSource Word for Windows and Excel Seminars

Arcus Pro-Stat 3

Radio Trac

Pro Tools Digital Audio 2

Apple System 7 Pro

ReelMagic video board

Indigo E-Print 1000

Microsoft Visual C+ +1.5

OLE 2

PC CAD software

50MHz DX2s

Kodaks Cineon

Sailmaking using computers

Visual Basic Tutorial

Converging the phone and the computer

Fuzzy Logic Chips

Publication Date: 1st March 1994

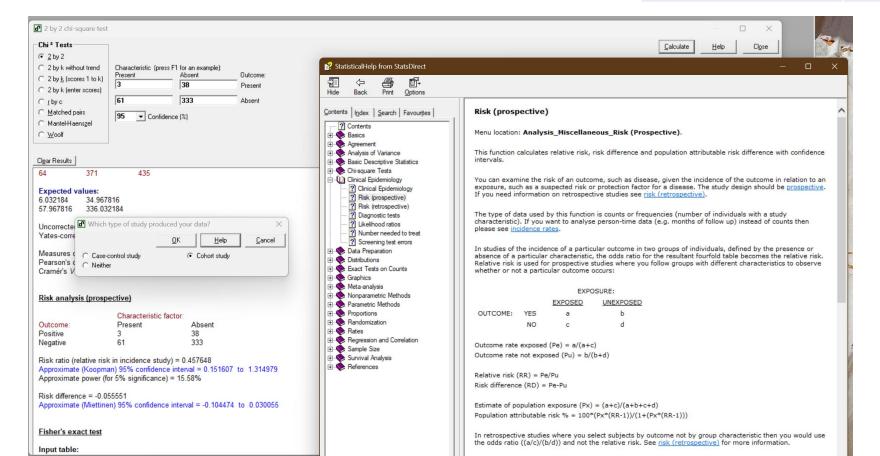


This exhibit has a reference ID of CH690. Please quote this reference ID in any communication with the Centre for Computing History.

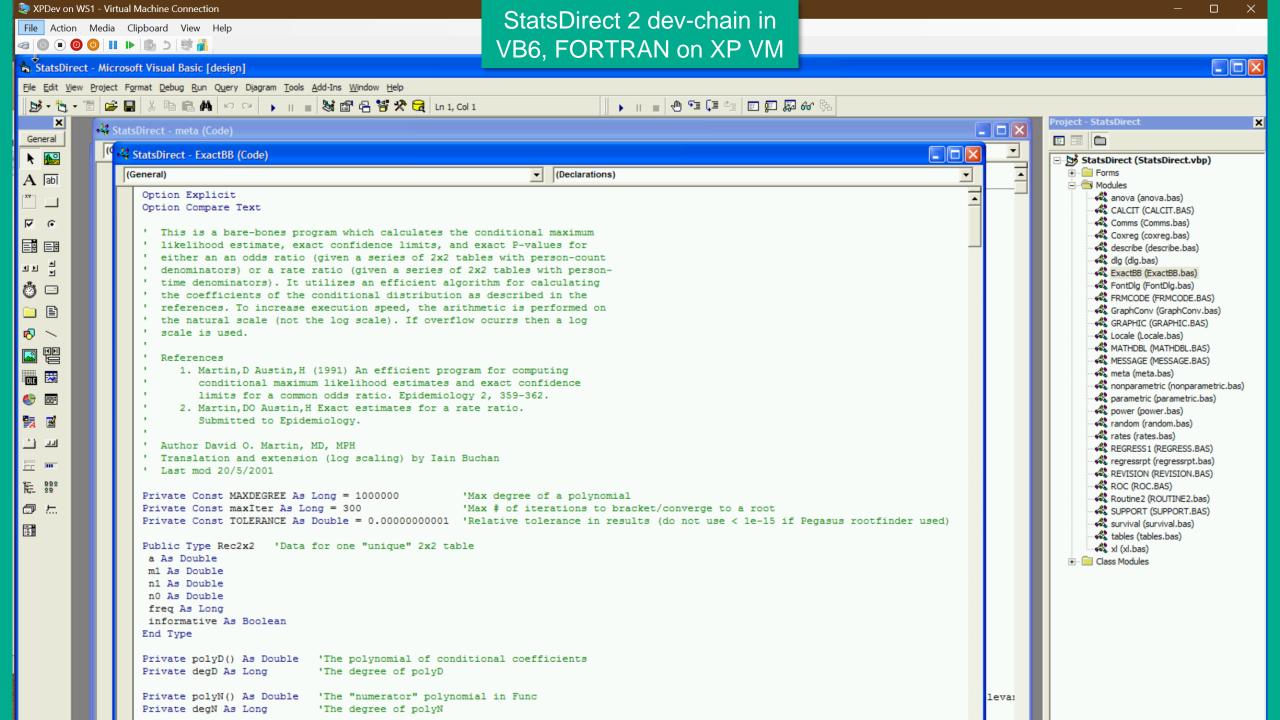
'Safe Statistics' - typical user correction

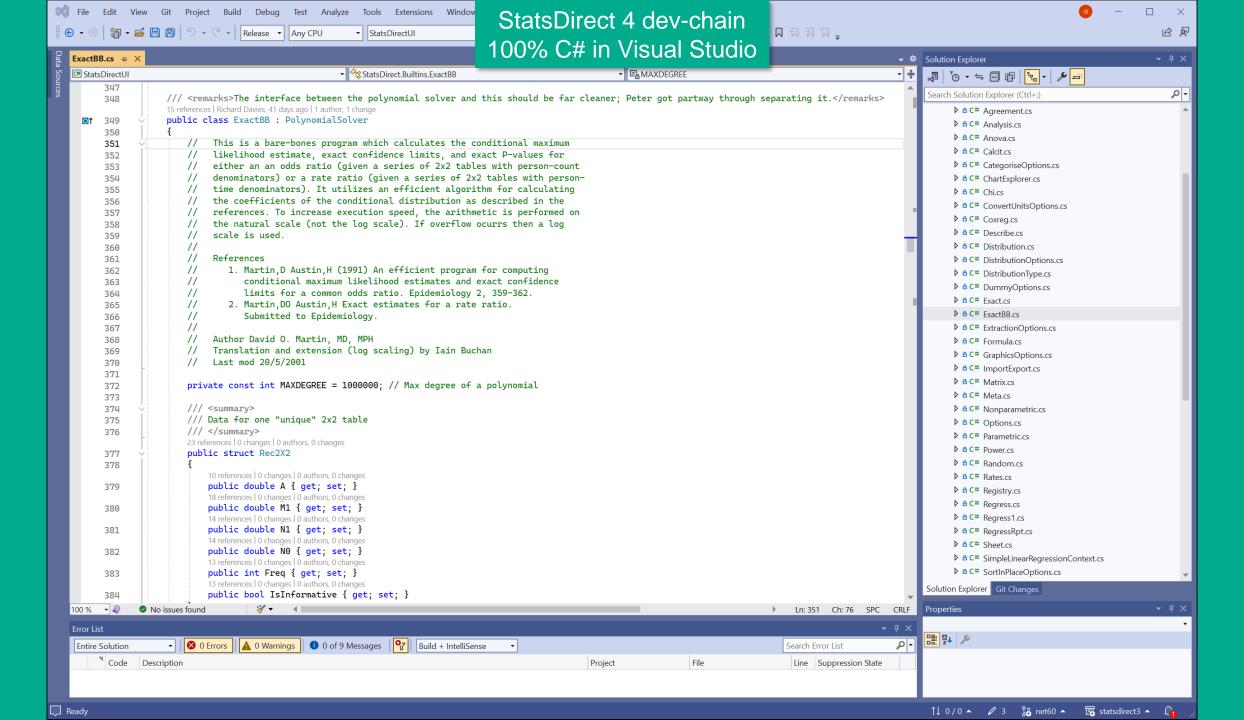
- Typical 2-by-2 table from clinical audit
- Medic wants chi-squared test, but needs relative risk confidence interval

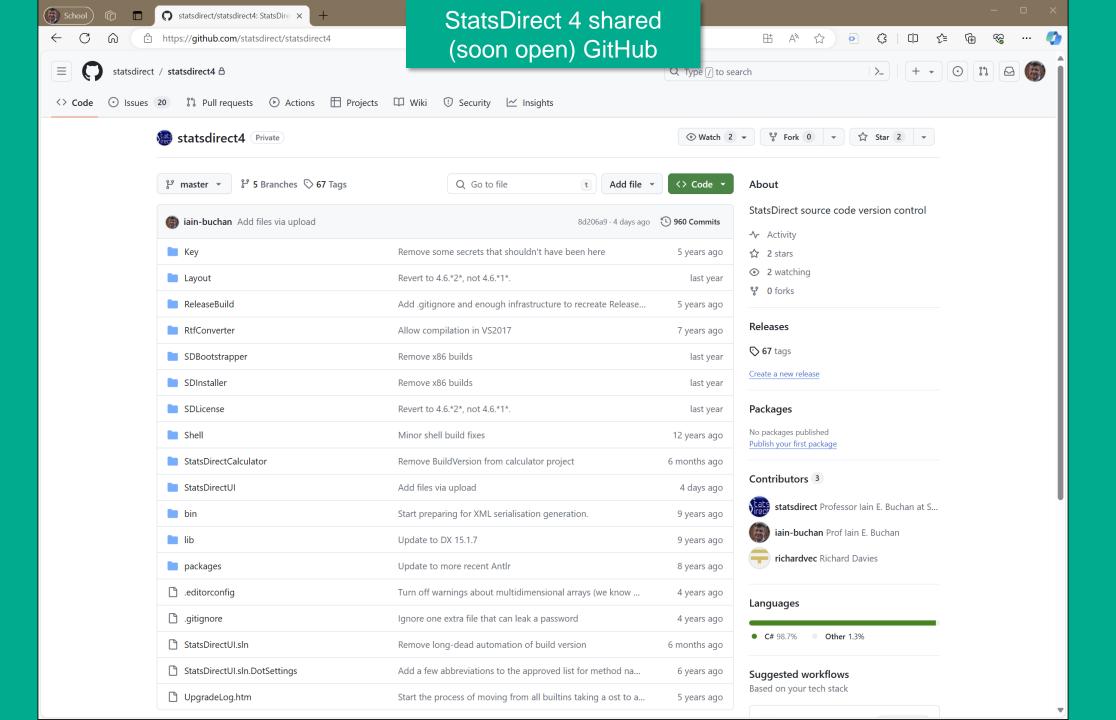
Exposure/ Outcome	New wound care	Usual wound care
Infected	3	38
Not infected	61	333

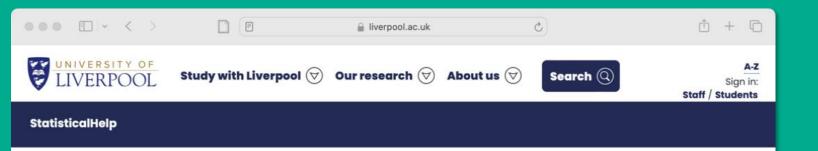


- From 20y old software (VB6, FORTRAN)
- User prompted to reflect on study design and correct method
- Help system helps interpret the right statistic: relative risk confidence interval not chi-square P-value









Software now free for unrestricted use

StatisticalHelp

University home > StatisticalHelp

StatisticalHelp is a set of free, open resources to help you learn and use biostatistical methods.

StatsDirect software

StatsDirect is an easy-to-use desktop application tuned to the statistical analysis needs of clinical and public health researchers and professionals.

You can download the software from the **StatsDirect website**. It runs on Windows devices capable of running .Net 6 or later, and on Macs via **Vmware Fusion** or **Parallels**.

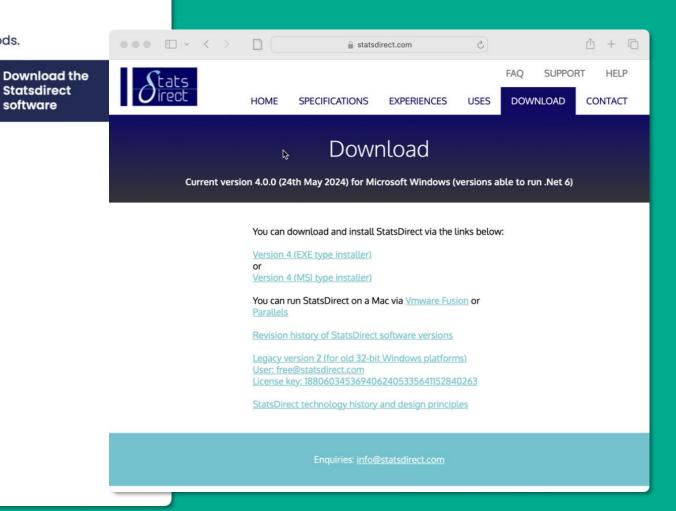
Biostatistical learning resources

The help system in StatsDirect is also a **learning resource**. Embedding this learning in an easy-to-use data analysis tool addresses the need for health experts who are infrequent users of statistical methods to re-learn basic principles as they explore data, in turn preparing them to interact with statisticians.

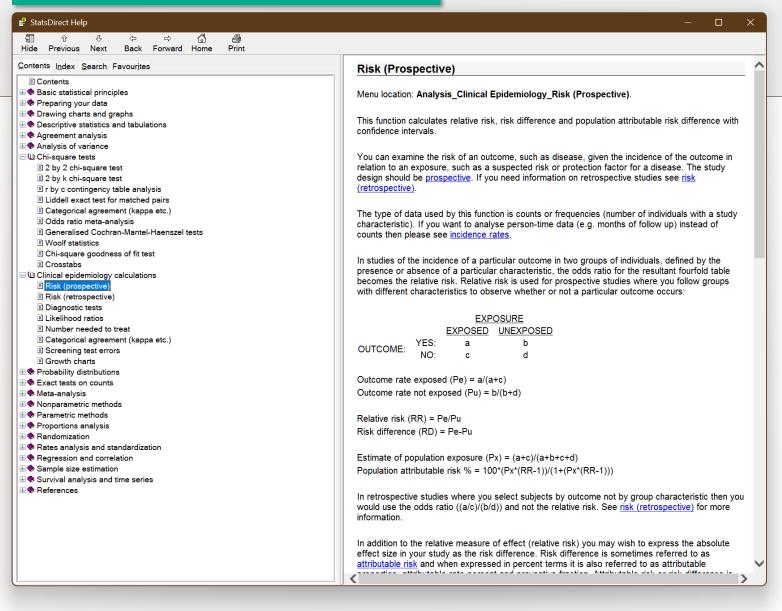
Benefits

This system is designed to make it easy to analyse data while improving your statistical knowledge. Benefits include:

- Quick and easy to use there's no programming required to use StatsDirect. The software uses interfaces that work like Microsoft Word and Excel. And it includes the statistical methods commonly used in health research.
- Supports your knowledge it provides a robust research tool that's good for learning and employs prompts and explanations that helps to overcome common statistical misconceptions.
- Reliable and trustworthy the software is a result of over 30 years of work and



StatsDirect 4 UX Auto-generated from XML 'functions'



Code-base History (<u>www.statsdirect.com/technology.aspx</u>)

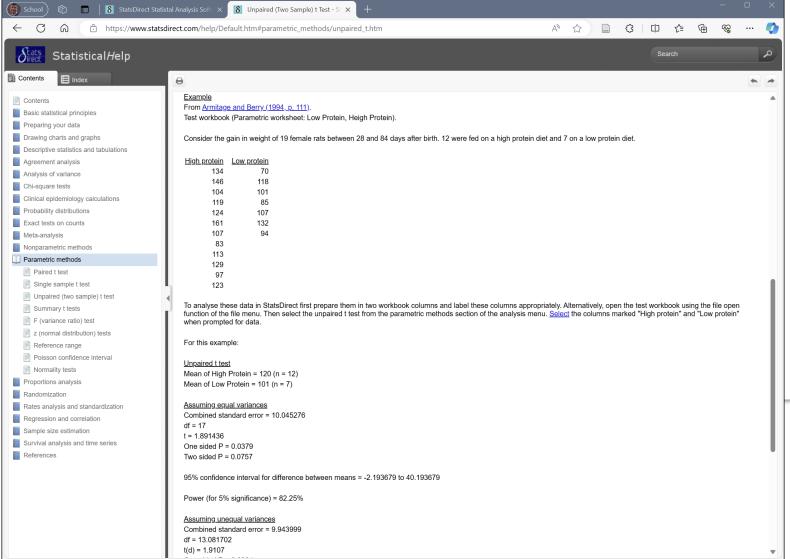
- 1987-2000: Gen 1 for MSDOS in BASIC PDS 7.1, FORTRAN, MS assembler no external components hand crafted spreadsheet
- 2000-2013: Gen 2 for Windows in VB6, FORTRAN external spreadsheet and report editor for familiar UX
- 2013-2024: Gen 3 for Windows on .Net Framework in C# similar spreadsheet and report editor external components
- 2024-: Gen 4 for Windows on .Net 6.1 in C# external components easily replaced – aiming for cross-platform (easy refactor)
- 2025...: Generative AI integration with help system to wean advanced users onto deeper analytic programming in R

StatsDirect 4 Coding Priorities 2024

- Replace CHM with HTML5 help (content ready at https://github.com/iain-buchan/statisticalhelp needs integrating)
- Move report editor from RTF/WMF to HTML/SVG (classes written) by shifting from DevExpress RichEdit to https://developer.microsoft.com/en-gb/microsoft-edge/webview2/ with https://www.tiny.cloud/
- Continue cross-platform preparation
- Explore native MacOS options
- Explore browser-based simple function embedding in HTML5 help system (Madcap Flare project above)



Conversational Data Analytics



```
Write me the R code for comparing these two groups using an unpaired, two-sample Student t-test
High protein Low protein
134 70
146 118
104 101
119 85
124 107
161 132
107 94
83
113
129
97
```

© Certainly! Below is the R code for performing an unpaired, two-sample Student t-test on the two groups "High protein" and "Low protein":

```
# Create vectors for the two groups
high_protein <- c(134, 146, 104, 119, 124, 161, 107, 83, 113, 129, 97, 123)
low_protein <- c(70, 118, 101, 85, 107, 132, 94)

# Perform the unpaired two-sample t-test
t_test_result <- t.test(high_protein, low_protein, var.equal = TRUE)

# Print the result
print(t_test_result)
```

This code assumes that the variances of the two groups are equal. If you suspect that the variances might not be equal, you can use `var.equal $\stackrel{\checkmark}{=} \Psi_{\text{ALSE}}$ ' instead.

Two Sample t-test

Question from a user who knows what method to use but doesn't have enough R coding skills to get started...

```
Compare these two groups using an unpaired, two-sample Student t-test
High protein Low protein
134 70
146 118
104 101
119 85
124 107
161 132
107 94
83
113
129
97
123
```

Certainly! I'll run an unpaired, two-sample Student t-test on the provided data using R. Below is the R code for this analysis, along with the steps to handle the missing data in the "Low protein" group.

```
# Create vectors for the two groups
high_protein <- c(134, 146, 104, 119, 124, 161, 107, 83, 113, 129, 97, 123)
low_protein <- c(70, 118, 101, 85, 107, 132, 94)

# Perform the unpaired two-sample t-test
t_test_result <- t.test(high_protein, low_protein, var.equal = TRUE)

# Print the result
print(t_test_result)
```

To provide a complete result, I'll explain how to interpret the output once you run the code in your R environment.

Interpretation of the t-test Result

When you run the above code, you'll get an output similar to this:



Key Components of the Output

- 1. t-value: This is the calculated t-statistic.
- 2. **degrees of freedom (df)**: This indicates the number of independent values that can vary in the
- 3. **p-value**: This value helps you determine the statistical significance of your results.
 - If the p-value is less than the significance level (commonly 0.05), you reject the null hypothesis, indicating a significant difference between the two groups.
- Confidence Interval This gives you a range within which the true difference between the group means lies with 95% confidence.
- Means of x and y: These are the mean values of the "High protein" and "Low protein" groups, respectively.

To run this test with unequal variances you can modify the `var.equal` parameter:

Running either version of the test will allow you to compare the two groups and determine if there is a significant difference between their means.



User thinks a P-value < 0.05 is the answer to their question as a "statistically significant": not so in this example, however, given more knowledge support they would place more emphasis on the width of the confidence interval and consider collecting more data

Statistical knowledge support needs conversation segways for different users

3 patients with a new wound care regime got infected where 61 did not, where 38 patients with the usual wound care regime got infected where 333 did not, is there a statistically significant difference?

To determine if there is a statistically significant difference between the infection rates of the two wound care regimes, we can perform a hypothesis test for the difference between two proportions. In this case, we can use a two-proportion z-test. Let's define the groups as follows:

Group 1: New wound care regime

• Infected: $x_1 = 3$ • Not infected: $n_1 - x_1 = 61$

• Total: $n_1 = 3 + 61 = 64$

• Group 2: Usual wound care regime • Infected: $x_2 = 38$

• Not infected: $n_2 - x_2 = 333$

• Total: $n_2 = 38 + 333 = 371$

We will test the null hypothesis H_0 that there is no difference between the proportions of infections

The steps are as follows:

• $\hat{p}_1 = \frac{x_1}{n_1} = \frac{3}{64}$ • $\hat{p}_2 = \frac{x_2}{n_2} = \frac{38}{371}$

2. Calculate the combined proportion \hat{p} :

1. Calculate the sample proportions:

• $\hat{p} = \frac{x_1 + x_2}{n_1 + n_2} = \frac{3 + 38}{64 + 371}$

3. Calculate the standard error (SE) of the difference between the two proportions:

in the two regimes, against the alternative hypothesis H_a that there is a difference.

•
$$SE = \sqrt{\hat{p} \cdot (1 - \hat{p}) \cdot \left(rac{1}{n_1} + rac{1}{n_2}
ight)}$$
 $iguplus$

• $z=\frac{\hat{p}_1-\hat{p}_2}{GE}$

4. Calculate the z-score:

Let's perform these calculations.

0.05) to decide if we reject the null hypothesis.

5. Determine the p-value from the z-score and compare it to the significance level (commonly

Here are the results of the calculations:

1. Sample proportions:

• Proportion of infections with the new wound care regime (\hat{p}_1) : 0.046875 • Proportion of infections with the usual wound care regime (\hat{p}_2): 0.1024

2. Combined proportion (\hat{p}):

• 0.0943

3. Standard error (SE): 0.0395

4. Z-score:

• -1.405

5. P-value:

• 0.1601

3 patients on a new wound care regimen got infected when 61 did not, and 38 patients with usual wound care got infected when 333 did not, is there a statistically significant difference?

Since the p-value (0.1601) is greater than the common significance level ($\alpha=0.05$), we fail to

reject the null hypothesis. This means there is no statistically significant difference between the

infection rates of the new wound care regime and the usual wound care regime. [-]

To calculate the relative risk (RR) and its 95% confidence interval, we'll use the following steps:

show me this as a relative risk with 95% confidence interval

1. Calculate the relative risk (RR):

$$RR=rac{p_1}{\hat{p}_2}$$
 where \hat{p}_1 is the infection rate for the new wound care regime and \hat{p}_2 is the infection rate for the

usual wound care regime. 2. Calculate the standard error (SE) of the log of the relative risk:

 $SE(\ln(RR)) = \sqrt{\frac{1}{x_1} - \frac{1}{n_1} + \frac{1}{x_2} - \frac{1}{n_2}}$

3. Calculate the 95% confidence interval for
$$\ln(RR)$$
:

$$\ln(CI) = \ln(RR) \pm Z imes SE(\ln(RR))$$

where Z is the z-value for a 95% confidence interval (approximately 1.96).

4. Exponentiate the bounds to obtain the 95% confidence interval for the relative risk:

$$CI = \left(e^{\ln(CI_{ ext{lower}})}, e^{\ln(CI_{ ext{upper}})}
ight)$$

Let's perform these calculations

Here are the results for the relative risk and its 95% confidence interval:

1. Relative Risk (RR):

$$RR=0.458$$

2. 95% Confidence Interval for RR:

This means that the relative risk of infection with the new wound care regime compared to the usua wound care regime is approximately 0.458. The 95% confidence interval ranges from 0.146 to 1.438, indicating that we do not have enough evidence to conclusively state that the new wound care regime significantly reduces or increases the not of infection compared to the usual regime, as the

show me this as a relative risk with 95% confidence interval

To calculate the relative risk (RR) and its 95% confidence interval, we'll use the following steps:

1. Calculate the relative risk (RR):

$$RR=rac{\hat{p}_1}{\hat{p}_2}$$

where \hat{p}_1 is the infection rate for the new wound care regime and \hat{p}_2 is the infection rate for the usual wound care regime.

2. Calculate the standard error (SE) of the log of the relative risk:

$$SE(\ln(RR)) = \sqrt{rac{1}{x_1} - rac{1}{n_1} + rac{1}{x_2} - rac{1}{n_2}}$$

3. Calculate the 95% confidence interval for $\ln(RR)$:

$$\ln(CI) = \ln(RR) \pm Z \times SE(\ln(RR))$$

where Z is the z-value for a 95% confidence interval (approximately 1.96).

4. Exponentiate the bounds to obtain the 95% confidence interval for the relative risk:

$$CI = \left(e^{\ln(CI_{ ext{lower}})}, e^{\ln(CI_{ ext{upper}})}
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Let's perform these calculations.

Here are the results for the relative risk and its 95% confidence interval:

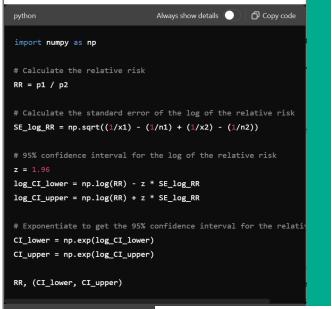
1. Relative Risk (RR):

$$RR = 0.458$$

2. 95% Confidence Interval for RR:

This means that the relative risk of infection with the new wound care regime compared to the usual wound care regime is approximately 0.458. The 95% confidence interval ranges from 0.146 to 1.438, indicating that we do not have enough evidence to conclusively state that the new wound care regime significantly reduces or increases the n_{∞}^{\downarrow} of infection compared to the usual regime, as the

rval Analysis



Risk analysis (prospective) (0.4576480263157895, (0.1456203 Characteristic factor: Outcome: Present Absent Positive 3 38 61 333 Negative Risk ratio (relative risk in incidence study) = 0.457648 Approximate (Koopman) 95% confidence interval = 0.151607 to 1.314979 Approximate power (for 5% significance) = 15.58% **Analysis** Risk difference = -0.055551

Approximate (Miettinen) 95% confidence interval = -0.104474 to 0.030055

 \times

Calculate the Koopman method confidence interval for RR

Lower bound

CI_lower_koopman = RR * np.exp(-1.96 * np.sqrt((1/x1) + (1/x2)))

Upper bound

CI_upper_koopman = RR * np.exp(1.96 * np.sqrt((1/x1) + (1/x2)))

(RR, (CI_lower_koopman, CI_upper_koopman))

(0.4576480263157895, (0.14127009512778288, 1.4825622917666437)

use the koopman method for the confidence interval

The Koopman method for calculating the confidence interval for the relative risk (RR) involves using the exact method for the binomial distribution. This approach is often more accurate for small sample sizes or when the event rates are low.

Here's how we can calculate the confidence interval for RR using the Koopman method:

1. Calculate the relative risk (RR):

$$RR=rac{\hat{p}_1}{\hat{p}_2}$$

where \hat{p}_1 is the infection rate for the new wound care regime and \hat{p}_2 is the infection rate for the usual wound care regime.

2. Calculate the lower and upper bounds for the confidence interval using the Koopman method:

$$ext{Lower bound} = rac{\hat{p}_1}{\hat{p}_2} \cdot e^{-1.96 \cdot \sqrt{rac{1}{x_1} + rac{1}{x_2}}}$$

$$ext{Upper bound} = rac{\hat{p}_1}{\hat{p}_2} \cdot e^{1.96 \cdot \sqrt{rac{1}{x_1} + rac{1}{x_2}}}$$

Using the Koopman method, the relative risk (RR) and its 95% confidence interval are as follows:

Relative Risk (RR):

$$RR = 0.458$$

2. 95% Confidence Interval for RR (Koopman method):

This means that the relative risk of infection with the new wound care regime compared to the usual wound care regime is approximately 0.458. The 95% confidence interval, calculated using the Koopman method, ranges from 0.141 to 1.483. In interval still includes 1.0, indicating that we do

use the koopman method for the confidence interval

The Koopman method for calculating the the exact method for the binomial distribusample sizes or when the event rates are left.

Analysis

Always show details 🔵 🗍 Copy code

X

Here's how we can calculate the confidence # Calculate the Koopman method confidence interval for RR

Calculate the relative risk (RR):

Lower boun

CI_lower_koopman = RR * np.exp(-1.96 * np.sqrt((1/x1) + (1/x2)))

Upper bound
CI_upper_koopman = RR * np.exp(1.96 * np.sqrt((1/x1) + (1/x2)))

(RR, (CI_lower_koopman, CI_upper_koopman))

Calculate the lower and upper bound method:

usual wound care regime.

where \hat{p}_1 is the infection rate for the i

(0.4576480263157895, (0.14127009512778288, 1.4825622917666437)

$$ext{Lower bound} = rac{\hat{p}_1}{\hat{p}_2} \cdot e^{-1.96 \cdot \sqrt{rac{1}{x_1} + rac{1}{x_2}}}$$

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Let's perform these calculations.

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Let Y_1 and Y_2 be multinomial random variables with parameters n_1, π_{1i} , and n_2, π_{2i} , respectively; where $i = \{1, 2, 3, \dots, r\}$. This encompasses the binomial case in which r = 1. We define the true selection ratio for the *i*th resource of *r* total resources to be:

$$heta_i = rac{\pi_{1i}}{\pi_{2i}}$$

2

where π_{1i} and π_{2i} represent the proportional use and availability of the *i*th resource, respectively. Note that if r=1 the selection ratio becomes relative risk. The maximum likelihood estimators for π_{1i} and π_{2i} are the sample proportions:

← Hallucinated

R: Confidence intervals for the ral X

$$\hat{\pi}_{1i}=rac{y_{1i}}{n_1},$$

$$\hat{\pi}_{2i}=rac{y_{2i}}{n_2}$$

where y_{1i} and y_{2i} are the observed counts for use and availability for the *i*th resource. The estimator for θ_i is:

$$\hat{ heta}_i = rac{\hat{\pi}_{1i}}{\hat{\pi}_{2i}}.$$

Method Algorithm

Katz-log
$$\hat{ heta}_i imes \exp(\pm z_1 - lpha/2\hat{\sigma}_W),$$

where
$$\hat{\sigma}_W^2 = rac{(1-\hat{\pi}_{1i})}{\hat{\pi}_{1i}n_1} + rac{(1-\hat{\pi}_{2i})}{\hat{\pi}_{2i}n_2}$$
.

Adjusted-log
$$\hat{\theta}_{Ai} \times \exp(\pm z_1 - \alpha/2\hat{\sigma}_A)$$
.

where
$$\hat{\theta}_{Ai} = \frac{y_{1i} + 0.5/n_1 + 0.5}{y_{1i} + 0.5/n_2 + 0.5}$$
,

$$\hat{\sigma}_A^2 = \frac{1}{y_1 + 0.5} - \frac{1}{n_1 + 0.5} + \frac{1}{y_2 + 0.5} - \frac{1}{n_2 + 0.5}.$$

Bailey
$$\hat{\theta}_i \left[\frac{1 \pm z_1 - (\alpha/2) \left(\hat{\pi}'_{1i}/y_{1i} + \hat{\pi}'_{2i}/y_{2i} - z_1 - (\alpha/2)^2 \hat{\pi}'_{1i} \hat{\pi}'_{2i}/9y_{1i}y_{2i} \right)^{1/2}/3}{1 - z_{1 - (\alpha/2)^2} \hat{\pi}'_{2i}/9y_{2i}} \right]^3,$$

where
$$\hat{\pi}'_{1i} = 1 - \hat{\pi}_{1i}$$
, and $\hat{\pi}'_{2i} = 1 - \hat{\pi}_{2i}$.

Inv. hyperbolic sine
$$\ln(\hat{ heta}_i) \pm \left[2sinh^{-1}\left(rac{z_{(1-lpha/2)}}{2}\sqrt{rac{1}{y_{1i}}-rac{1}{n_1}+rac{1}{y_{2i}}-rac{1}{n_2}}
ight)
ight],$$

Koopman Find
$$X^2(\theta_0) = \chi_1^2(1-\alpha)$$
, where

$$ilde{\pi}_{1i} = rac{ heta_0(n_1 + y_{2i}) + y_{1i} + n_2 - [\{ heta_0(n_1 + y_{2i}) + y_{1i} + n_2\}^2 - 4 heta_0(n_1 + n_2)(y_{1i} + y_{2i})]^{0.5}}{2(n_1 + n_2)},$$

$$ilde{\pi}_{2i} = rac{ ilde{\pi}_{1i}}{ heta_0}, ext{ and } X^2(heta_0) = rac{(y_{1i} - n_1 ilde{\pi}_{1i})^2}{n_1 ilde{\pi}_{1i} (1 - ilde{\pi}_{1i})} igg\{ 1 + rac{n_1 (heta_0 - ilde{\pi}_{1i})}{n_2 (1 - ilde{\pi}_{1i})} igg\}.$$

Noether $\hat{\theta}_i \pm z_1 - \alpha/2\hat{\sigma}_N$,

where
$$\hat{\sigma}_N^2 = \hat{ heta}_i^2 \left(rac{1}{y_{1i}} - rac{1}{n_1} + rac{1}{y_{2i}} - rac{1}{n_2}
ight)$$
.

Slight tweak to question and different ChatGPT4 session:

3 patients on a new wound care regimen got infected when 61 did not, where 38 patients with usual wound care got infected when 333 did not, is there a statistically significant difference?

To determine if there is a statistically significant difference between the infection rates of the two wound care regimens, we can perform a chi-square test of independence. This test will help us understand if the observed differences in infection rates between the two groups are due to chance or if there is a statistically significant association between the type of wound care regimen and infection rates.

Let's set up the contingency table based on the given data:

	Infected	Not Infected	Total
New Wound Care Regimen	3	61	64
Usual Wound Care	38	333	371
Total	41	394	435

Now, we'll perform the chi-square test.

The chi-square test statistic is approximately 1.38, and the p-value is approximately 0.24.

Since the p-value is greater than the common significance level of 0.05, we fail to reject the null hypothesis. This means there is no statistically significant difference in infection rates between the new wound care regimen and the usual wound care regimen. The observed difference in infection rates could be due to chance. [>-]

c.f. ...

3 patients with a new wound care regime got infected where 61 did not, where 38 patients with the usual wound care regime got infected where 333 did not, is there a statistically significant difference?

To determine if there is a statistically significant difference between the infection rates of the two wound care regimes, we can perform a hypothesis test for the difference between two proportions. In this case, we can use a two-proportion z-test.

Let's define the groups as follows:

- Group 1: New wound care regime
 - Infected: $x_1 = 3$
 - Not infected: $n_1 x_1 = 61$
 - Total: $n_1 = 3 + 61 = 64$
- Group 2: Usual wound care regime
 - Infected: $x_2 = 38$
 - Not infected: $n_2-x_2=333$
 - Total: $n_2 = 38 + 333 = 371$

We will test the null hypothesis H_0 that there is no difference between the proportions of infections in the two regimes, against the alternative hypothesis H_a that there is a difference.

The steps are as follows:

- 1. Calculate the sample proportions:
 - $\hat{p}_1 = \frac{x_1}{n_1} = \frac{3}{64}$
 - $\hat{p}_2 = \frac{x_2}{n_2} = \frac{38}{371}$
- 2. Calculate the combined proportion \hat{p} :
 - $\hat{p} = \frac{x_1 + x_2}{n_1 + n_2} = \frac{3 + 38}{64 + 371}$
- 3. Calculate the standard error (SE) of the difference between the two proportions:

•
$$SE = \sqrt{\hat{p} \cdot (1 - \hat{p}) \cdot \left(rac{1}{n_1} + rac{1}{n_2}
ight)}$$
 $iguplus$

1. Relative Risk (RR):

$$RR = \frac{\text{Incidence rate in the treatment group}}{\text{Incidence rate in the control group}} = \frac{\frac{3}{64}}{\frac{38}{371}}$$

2. Standard Error (SE) for log(RR):

$$SE=\sqrt{rac{1}{a}-rac{1}{a+b}+rac{1}{c}-rac{1}{c+d}}$$

where:

- 1. Compute the relative risk:
- a is the number of infected in the treat
- b is the number of not infected in the
- c is the number of infected in the con
- d is the number of not infected in the

Semantic equivalence

Same asymptotic approximation of variance reported when alternative methods requested

$$RR=rac{a/(a+b)}{c/(c+d)}$$

2. Compute the confidence interval using the following bounds:

$$ext{Lower bound} = rac{RR}{\exp(ext{SE} \cdot Z_{lpha/2})}$$

$$ext{Upper bound} = rac{RR}{\exp(- ext{SE} \cdot Z_{lpha/2})}$$

where $Z_{\alpha/2}$ is the critical value from the standard normal distribution for a 95% confidence interval (typically 1.96).

Let's perform these calculations.

The relative risk (RR) is approximately 0.46, and the 95% confidence interval calculated using the Koopman method is (0.15, 1.44).

This confidence interval is the same as the one obtained earlier, indicating that the infection rate for the new wound care regimen is not statistically significantly different from the usual wound care regimen, with considerable uncertainty about the true effect.

show me this as a relative risk with 95% confidence interval

To calculate the relative risk (RR) and its 95% confidence interval, we'll use the following steps:

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where \hat{p}_1 is the infection rate for the new wound care regime and \hat{p}_2 is the infection rate for the usual wound care regime.

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Statistica/Help Test Battery for Generative Als

- At the end of each <u>www.statisticalhelp.org</u> worked example add a 'chat' that reproduces the answers given the data and question
- Compare ChatGPT and Gemini, varying hallucination settings
- Give a red (failed), amber (part-answered) and green (answered) rating for the Als tested (by version and date)
- Construct an overall score from a battery of ratings
- Consider how to jump in and out of a generative AI supported by best practice statistical examples matching the user's data/questions



Thank You

To collaborate in the StatisticalHelp challenge email buchan@liverpool.ac.uk and join our GitHub projects



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